

## Assignment 8

Due date: 28 May 2021

TA: 林宏懌 E817 (13:10~14:00)

1. Find the values of  $k$  for which the matrix  $A$  is invertible.

$$A = \begin{bmatrix} 1 & 2 & 0 \\ k & 1 & k \\ 0 & 2 & 1 \end{bmatrix}.$$

2. Prove that a square matrix  $A$  is invertible if and only if  $A^T A$  is invertible.
3. Prove that if  $A$  is a square matrix, then

$$\det(A^T A) = \det(AA^T).$$

4. Show that the matrix

$$A = \begin{bmatrix} \cos \theta & \sin \theta & 0 \\ -\sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

is invertible for all values of  $\theta$ . Then, find  $A^{-1}$ .