Quiz 2

Due date: 15 May 2024

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- 1. (25%) Suppose that \mathbf{u} , \mathbf{v} , and \mathbf{w} are vectors such that inner product $\langle \mathbf{u}, \mathbf{v} \rangle = 2$, $\langle \mathbf{v}, \mathbf{w} \rangle = -3$ and $\langle \mathbf{u}, \mathbf{w} \rangle = 1$. Moreover, the norms $\|\mathbf{u}\| = 1$, $\|\mathbf{v}\| = 2$, $\|\mathbf{w}\| = 5$. Please compute the value of $\langle 2v w, 3u + 2w \rangle$.
- 2. (25%) Find the adjoint of the matrix $A = \begin{bmatrix} 1 & -1 & 0 \\ 5 & -4 & 3 \\ 2 & 0 & -1 \end{bmatrix}$.
- 3. (25%) Find the $||\operatorname{proj}_{\mathbf{a}}\mathbf{u}||$, where $\mathbf{u}=(1,-2),\ \mathbf{a}=(-4,-3).$
- 4. (25%) Show that $||v||_1 \le \sqrt{n}||v||_2$ for any $v \in \mathbb{R}^n$. (*Hint: Using Cauchy–Schwarz inequality*)